

Selling Data to Agent with Endogenous Information

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Selling Information

Seller maximizes the revenue by selling information to a buyer.

Buyer is a decision maker who uses acquired information to improve the expected utility from better decisions.

- buyer has private value of information;
- buyer can endogenously acquire additional information.

Timeline:

- 1 Seller offers a menu for selling information.
- 2 Buyer chooses an option for buying information from seller.
- 3 Buyer receives a signal from the seller, and then purchase additional information endogenously from other sources.
- 4 Buyer makes a decision and final utility is realized.

Comparison to exogenous information:

buyer is endowed with additional information regardless of the selling mechanism.

Sequential-learning Proof

Buyer has costs for acquiring additional information.

- buyer can sequentially acquire any feasible information;
- expected cost of any sequential experiment is weakly higher than any single experiment that is equally informative.

Example: Gaussian Learning

- prior is Gaussian;
- acquire a signal with Gaussian noise with fixed cost $c > 0$.

Optimal Mechanisms

Theorem. *In the optimal mechanisms, the buyer has no incentive to acquire additional costly information in eqm.*

Comparative Statics:

- optimal revenue increases when the set of feasible information the buyer can purchase shrinks;
- optimal revenue increases when buyer's cost of acquiring additional information increases.

Linear Valuation

Buyer's value for information is separable between his private type and the improvement from refining posterior belief.

- expected value $V(\mu, \theta) = \theta \cdot v(\mu)$
 \Rightarrow value of info $V(\sigma, \mu, \theta) = \theta \cdot (\mathbf{E}_{\hat{\mu} \sim \sigma|D}[v(\hat{\mu})] - v(\mu));$

Example: matching utilities

- buyer with private type θ tries to predict unknown outcome;
- buyer receives value θ if the prediction is correct and 0 o.w.

Theorem. *Assuming linear valuation, in the optimal mechanisms, there is a threshold on the type such that*

- *higher types receives full information;*
- *low types receives partial information which is what they would purchase from other sources if the seller offers no information.*

Pricing for Full Information

Theorem (Exogenous Information [Bergemann, Cai, Velegkas, Zhao '21]) *Assuming linear valuation and regular distribution, for any $\epsilon > 0$, there exists an instance such that pricing for full information is at most ϵ fraction of the optimal revenue.*

Theorem (Endogenous Information) *Assuming linear valuation and regular distribution, pricing for full information achieves at least half of the optimal revenue.*

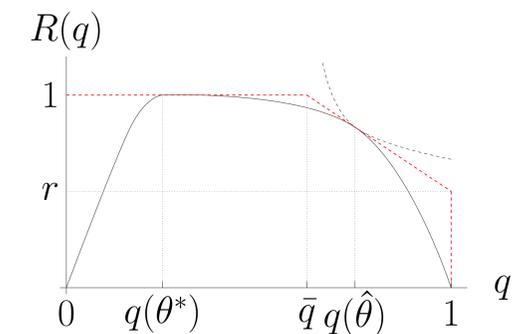


Figure: Reduction on identifying the type distribution that maximizes the approximation ratio between the optimal revenue and optimal pricing.

Interpretation:

- price discrimination is crucial if buyer's additional information is exogenous, but not crucial if it is endogenous.
- extreme information structure such that pricing is a bad approximation will not arise endogenously.

Working paper at [arXiv:2103.05788](https://arxiv.org/abs/2103.05788)